

# Subleading corrections to parity violating pion photoproduction

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## Abstract

We compute the photon asymmetry for near threshold parity violating (PV) pion photoproduction through sub-leading order. We find a potentially significant contribution from new PV low-energy constants not considered previously. We observe that a measurement of this asymmetry may help clarify the theoretical interpretation of backward angle PV electron-proton scattering, provided that the PV  $\pi NN$  Yukawa coupling is determined from nonradiative nuclear PV experiments.

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The parity violating (PV)  $\pi NN$  Yukawa coupling constant  $h_\pi^1$  is a key ingredient to the understanding of the PV nuclear interaction [1, 2, 3, 4, 5]. There have been a number of past attempts to extract this coupling from PV reactions [2, 5, 6, 7, 8, 9], and there are a slate of new experiments, suggested or being planned, with this goal in mind, *e.g.*,  $\bar{n}p \rightarrow d\gamma$  at LANSCE [10],  $\gamma d \rightarrow np$  at Jefferson Lab [11], the rotation of polarized neutrons in helium at NIST [9] as well as polarized Compton scattering processes [12, 13].

Recently, Chen and Ji (CJ) suggested using PV  $\pi^+$  photoproduction near threshold in order to extract  $h_\pi^1$  [14]. Specifically, the process considered by these authors is

$$\vec{\gamma}(q^\mu; \epsilon^\mu) + p(P_i^\mu) \rightarrow \pi^+(k^\mu) + n(P_f^\mu), \quad (1)$$

where  $q^\mu = (\omega, \mathbf{q})$ ,  $P_i^\mu$ ,  $k^\mu = (\omega_\pi, \mathbf{k})$ , and  $P_f^\mu$  are the center-of-mass four-momenta of photon, proton, pion and neutron, respectively, and  $\epsilon^\mu$  is the photon polarization vector. In the threshold region, the pion and photon as well as the nucleon momenta are much smaller than the chiral symmetry breaking scale  $\Lambda_\chi = 4\pi F_\pi \sim 1$  GeV and CJ demonstrated that the use of heavy baryon chiral perturbation theory [15, 16] yields a low energy theorem for the threshold PV photon-helicity asymmetry at lowest order of the chiral expansion:

$$A_\gamma(\omega_{\text{th}}, \theta) = \frac{\sqrt{2}F_\pi(\mu_p - \mu_n)}{g_A m_N} h_\pi^1, \quad (2)$$

The corrections from terms higher order in the chiral expansion were estimated to be around 20% [14]. This process has been studied from the point of view of a more conventional meson exchange approach in [17, 18], and the same  $h_\pi^1$  dominance of the asymmetry at threshold was found [18].

In this note we present the first order sub-leading result for the asymmetry. Contrary to the naive expectation that such higher order corrections are small, the subleading correction from the PV  $\pi NN$  vector coupling  $h_V$  (defined below) is of order unity, as previously found in the radiative corrections to  $h_\pi^1$  [19] and to the nucleon anapole moment [20]. We further argue that the proposed parity violating photoproduction process is more suitable for constraining  $h_V$  rather than  $h_\pi^1$ . In contrast, other – nonradiative – processes [9, 10, 11] may be most appropriate for the determination of  $h_\pi^1$ , since vector current conservation implies the contributions from  $h_V$  are suppressed in such cases. Finally we observe that the contribution from  $h_V$  to the nucleon anapole moment introduces significant theoretical uncertainty into the axial vector radiative correction  $R_A$  for backward angle PV  $ep$  scattering [20]. The SAMPLE collaboration has recently reported an result for this correction which appears to differ from the theoretical estimate [21]. A new constraint on  $h_V$  from PV pion photoproduction would reduce the theoretical uncertainty in  $R_A$  and may help resolve the apparent difference between theory and experiment.

The motivation behind the use of heavy baryon chiral perturbation theory (HBCPT) is explained in detail in [14], so we follow the notations of this reference. Since we work in the near-threshold region, we use the so-called “small-scale” expansion [22], *i.e.*, we treat  $\omega, \omega_\pi, |k|, m_\pi, \delta = m_\Delta - m_N$ , etc. as small quantities and characterize amplitudes by the number of powers of these terms, *e.g.*, we count the term  $\omega_\pi/q \cdot k$  as being  $\mathcal{O}(p^{-1})$ . The photon asymmetry arises from the interference of the parity conserving (PC) and PV amplitudes. In Ref. [14] the asymmetry was truncated at leading order, *i.e.*,  $\mathcal{O}(p^0)$ . In the present work we include the  $\mathcal{O}(p)$  correction, which arises dominantly from the PV vector  $\pi NN$

couplings. As we show later, the corrections from other low energy constants (LECs) like PV  $\gamma NN\pi$  vertices are likely to be small, as are other sub-leading contributions to the PV and PC amplitudes. Moreover, chiral loops contribute to the asymmetry only at  $\mathcal{O}(p^2)$  and higher. Hence, our truncation of the chiral expansion of the asymmetry is consistent and complete up to terms of  $\mathcal{O}(p)$ .

The PC amplitudes which describe the charged photoproduction reaction are defined via

$$T^{PC} = N^\dagger \left[ i\mathcal{A}_1 \sigma \cdot \epsilon + i\mathcal{A}_2 \sigma \cdot \hat{\mathbf{q}} \epsilon \cdot \hat{\mathbf{k}} + i\mathcal{A}_3 \sigma \cdot \hat{\mathbf{k}} \epsilon \cdot \hat{\mathbf{k}} + \mathcal{A}_4 \epsilon \cdot \hat{\mathbf{q}} \times \hat{\mathbf{k}} \right] N, \quad (3)$$

where  $N$  is the proton Pauli spinor,  $\sigma$  are the Pauli spin matrices, and  $\hat{\mathbf{q}}$  and  $\hat{\mathbf{k}}$  are the unit vectors in the photon and pion directions respectively. At leading order in HBCPT, we have  $\mathcal{A}_1 = eg_A/\sqrt{2}F_\pi$ ,  $\mathcal{A}_2 = \mathcal{A}_1\omega|\mathbf{k}|/q \cdot k$ ,  $\mathcal{A}_3 = -\mathcal{A}_1\mathbf{k}^2/q \cdot k$ , and  $\mathcal{A}_4 = 0$  [23, 24]. As explained in [14] one also requires the non-vanishing subleading order result for  $\mathcal{A}_4$ .

$$\mathcal{A}_4 = \frac{eg_A|\mathbf{k}|}{2\sqrt{2}F_\pi m_N} \left[ \mu_p - \left( \frac{\omega}{\omega_\pi} \right) \mu_n \right] - \frac{2eg_{\pi N\Delta}G_1|\mathbf{k}|}{9\sqrt{2}F_\pi m_N} \left( \frac{\omega}{\omega - \delta} + \frac{\omega}{\omega_\pi + \delta} \right), \quad (4)$$

where the  $\Delta(1232)$  contribution has been included explicitly. Here  $G_1$  is the M1 transition moment connecting the nucleon and delta, and  $g_{\pi N\Delta}$  is the  $\pi$ - $N$ - $\Delta$  coupling. Note that  $\mathcal{A}_{1-3}$  is  $\mathcal{O}(p^0)$  while  $\mathcal{A}_4$  is  $\mathcal{O}(p)$ .

To  $\mathcal{O}(p)$  in the chiral expansion, the PV  $\gamma p \rightarrow \pi^+ n$  T-matrix can be written as

$$T^{PV} = N^\dagger \left[ \mathcal{F}_1 \hat{\mathbf{k}} \cdot \epsilon + i\mathcal{F}_2 \sigma \cdot \epsilon \times \hat{\mathbf{q}} + i\mathcal{F}_3 \sigma \cdot \epsilon \times \hat{\mathbf{k}} \right] N. \quad (5)$$

We have then the asymmetry

$$A_\gamma \sim \{ \mathcal{A}_1 \mathcal{F}_2 + \frac{\sin^2 \theta}{2} [\mathcal{A}_3 \mathcal{F}_2 - \mathcal{A}_4 \mathcal{F}_1 - \mathcal{A}_2 \mathcal{F}_3] + \cos \theta \mathcal{A}_1 \mathcal{F}_3 \}, \quad (6)$$

where  $\theta = \cos^{-1} \hat{\mathbf{q}} \cdot \hat{\mathbf{k}}$ . The nominally leading piece from the interference term  $\mathcal{A}_{1-3}\mathcal{F}_1$  vanishes if the proton target is unpolarized.

The leading, nonvanishing contributions to  $A_\gamma$ , which occur at  $\mathcal{O}(p^0)$ , are generated by the  $\mathcal{O}(p^0)$  terms in  $\mathcal{A}_{1-3}$  interfering with the  $\mathcal{O}(p^0)$  terms in  $\mathcal{F}_2$ , and by the  $\mathcal{O}(p)$  term in  $\mathcal{A}_4$  interfering with the  $\mathcal{O}(p^{-1})$  term in  $\mathcal{F}_1$ . The leading order PV contributions to  $\mathcal{F}_{1,2}$  arise from the insertion of the PV Yukawa  $\pi NN$  vertex in FIG. 1 (a), (c), (d).

$$\mathcal{L}_{Yukawa}^{PV} = -ih_\pi^1 \pi^+ p^\dagger n + h.c. + \dots, \quad (7)$$

using the sign convention of Ref. [20, 19]. The radiative corrections to  $h_\pi^1$  were discussed extensively in [19], where it was pointed out that what nuclear PV experiments measure is an effective coupling  $h_\pi^{eff}$  [19], which is a linear combination of LECs  $h_\pi^1, h_\Delta, h_A^{(i)}$  etc. The commonly

used “best value”— $|h_\pi^1| = 5 \times 10^{-7}$ —quoted in [1] corresponds to a large extent to a simple tree-level estimate without loop corrections. The leading-order contribution from the PV Yukawa couplings to the photoproduction amplitudes are found to be [14]:

$$\mathcal{F}_1 = -\frac{eh_\pi^1|\mathbf{k}|}{q \cdot k}, \quad \mathcal{F}_2 = -\frac{eh_\pi^1}{2m_N} \left[ \mu_p - \left( \frac{\omega}{\omega_\pi} \right) \mu_n \right]. \quad (8)$$

where  $\mathcal{F}_1, \mathcal{F}_2$  are  $\mathcal{O}(p^{-1}), \mathcal{O}(p^0)$  respectively.

Subleading contributions to  $A_\gamma$  are generated by  $\mathcal{O}(p)$  and  $\mathcal{O}(p^2)$  terms in  $\mathcal{A}_{1-3}$  and  $\mathcal{A}_4$ , respectively, interfering with the amplitudes in Eq. (8), and by  $\mathcal{O}(p)$  contributions in  $\mathcal{F}_{2,3}$  interfering with the  $\mathcal{O}(p^0)$  terms in  $\mathcal{A}_{1-3}$ . The subleading PC contributions have been computed in [24]. We refer to the detailed expressions for these corrections in that work, which we employ in our numerical analysis below. Of greater interest are the  $\mathcal{O}(p)$  PV amplitudes involving new LEC’s. These contributions are generated by the following two Lagrangians:

$$\mathcal{L}_V^{PV} = -\frac{h_V}{\sqrt{2}F_\pi} \bar{p} \gamma^\mu n D_\mu \pi^+ + h.c. + \dots \quad (9)$$

$$\mathcal{L}_{\gamma NN\pi}^{PV} = -ie \frac{C}{\Lambda_\chi F_\pi} \bar{p} \sigma^{\mu\nu} F_{\mu\nu} n \pi^+ + h.c. \quad (10)$$

where  $h_V = h_V^0 + \frac{4}{3}h_V^2$  in terms of the couplings defined in [19]. We note that the expressions in Eqs. (9, 10) represent only the one-pion term in an expansion of the nonlinear PV Lagrangians of Refs. [4, 19].

These new PV vertices contribute to both the pole diagrams FIG. 1 (c), (d) and the seagull diagram FIG. 1 (b). From the former we have

$$\mathcal{F}_1^{pole} = -\frac{eh_V|\mathbf{k}|}{\sqrt{2}F_\pi m_N}, \quad \mathcal{F}_2^{pole} = -\frac{eh_V}{2m_N} \frac{\omega_\pi}{\sqrt{2}F_\pi} \left[ \mu_p - \left( \frac{\omega}{\omega_\pi} \right) \mu_n \right]. \quad (11)$$

From the seagull diagram we find

$$\mathcal{F}_1^{seagull} = -\frac{eh_V|\mathbf{k}|}{2\sqrt{2}F_\pi m_N}, \quad \mathcal{F}_2^{seagull} = -e \left[ \frac{h_V}{2\sqrt{2}m_N} + \frac{2C}{\Lambda_\chi} \right] \frac{\omega}{F_\pi}, \quad \mathcal{F}_3^{seagull} = \frac{eh_V}{2m_N} \frac{|\mathbf{k}|}{\sqrt{2}F_\pi}. \quad (12)$$

Note that the  $h_V$  contribution to  $\mathcal{F}_1$  is always two orders higher than that from  $h_\pi^1$ . Thus, since we truncate the asymmetry at  $\mathcal{O}(p)$ , the terms  $\mathcal{F}_1^{pole}, \mathcal{F}_1^{seagull}$  can be safely discarded.

In addition to the  $\mathcal{O}(p)$  contributions from  $h_V$  and  $C$ ,  $\mathcal{F}_2$  receives an  $\mathcal{O}(p)$  contribution involving  $h_\pi^1$  generated by the  $1/m_N$  corrections to the nucleon propagator and  $\gamma NN$  vertex in the pole amplitudes. We include these corrections in the asymmetry formulae below. Other possible

contributions to the PV amplitudes include PV  $\gamma N\Delta$  and  $\pi N\Delta$  interactions. However, both contribute at  $\mathcal{O}(p^2)$ , which is higher than the order at which we are truncating. Similarly chiral loop contributions to  $\mathcal{A}_{1-4}$ ,  $\mathcal{F}_1$ ,  $\mathcal{F}_2$ ,  $\mathcal{F}_3$  appear at  $\mathcal{O}(p^2)$ ,  $\mathcal{O}(p)$ ,  $\mathcal{O}(p^2)$  or higher, respectively. Consequently, chiral loops do not contribute to the asymmetry until at least  $\mathcal{O}(p^2)$ . All such contributions are then higher order and can be dropped.

Thus the photon asymmetry at order  $\mathcal{O}(p)$  reads

$$\begin{aligned} A_\gamma(\omega, \theta) = & \frac{\sqrt{2}h_\pi^1 F_\pi}{g_A m_N \mathcal{G}} \left\{ \left[ \mu_p - \left( \frac{\omega}{\omega_\pi} \right) \mu_n \right] \left( 1 - \frac{\sin^2 \theta \mathbf{k}^2}{q \cdot k} \right) \right. \\ & + \frac{2}{9} \frac{g_{\pi N \Delta} G_1 \sin^2 \theta \mathbf{k}^2}{g_A q \cdot k} \left( \frac{\omega}{\omega - \delta} + \frac{\omega}{\omega_\pi + \delta} \right) \Big\} \\ & + \frac{h_V \omega_\pi}{g_A m_N \mathcal{G}} \left[ \mu_p - \left( \frac{\omega}{\omega_\pi} \right) \mu_n + \frac{\omega}{\omega_\pi} \right] \left( 1 - \frac{\sin^2 \theta \mathbf{k}^2}{2q \cdot k} \right) \\ & + \frac{4\sqrt{2}C\omega}{g_A \Lambda_\chi \mathcal{G}} \left( 1 - \frac{\sin^2 \theta \mathbf{k}^2}{2q \cdot k} \right) \\ & - \frac{|\mathbf{k}|}{g_A m_N \mathcal{G}} \left[ h_V - \frac{2\sqrt{2}F_\pi \omega}{m_N \omega_\pi} \mu_n h_\pi^1 \right] \left( \cos \theta - \frac{\sin^2 \theta \omega |\mathbf{k}|}{2q \cdot k} \right) \\ & - \frac{h_\pi^1 F_\pi \omega}{\sqrt{2} g_A m_N^2 \mathcal{G}} \left[ \mu_p - \left( \frac{|\mathbf{k}|^2}{\omega_\pi^2} \right) \mu_n \right] \left( 1 - \frac{\sin^2 \theta \mathbf{k}^2}{2q \cdot k} \right) + \dots \quad (13) \end{aligned}$$

where  $\mathcal{G} = 1 - \frac{\sin^2 \theta |\mathbf{k}|^2}{q \cdot k} \left[ 1 - \frac{(\mathbf{q} - \mathbf{k})^2}{2q \cdot k} \right]$  and where the ellipses indicate the subleading PC contributions of [24].

At threshold— $|\mathbf{k}| = \mathbf{0}$ —we find the low energy theorem for the photon asymmetry at  $\mathcal{O}(p)$ :

$$\begin{aligned} A_\gamma(\omega_{\text{th}}, \theta) = & \frac{\sqrt{2}F_\pi}{g_A m_N} \left[ \mu_p - \mu_n \left( 1 + \frac{m_\pi}{2m_N} \right) \right] h_\pi^1 \\ & + \frac{m_\pi(\mu_p - \mu_n + 1)}{g_A m_N} h_V + \frac{4\sqrt{2}m_\pi}{g_A \Lambda_\chi} C \quad (14) \end{aligned}$$

We observe that the original low energy theorem, Eq. (2), receives a nearly 100% correction from the PV vector coupling  $h_V$ , since  $h_V$  and  $h_\pi^1$  may be comparable[4, 20].

There thus exist three separate unknown LEC's in the asymmetry formula, each with its distinct energy dependence and angular distribution, as indicated in FIG. 2. In principle, one might be able to separate  $h_\pi^1$ ,  $h_V$ , and  $C$  by exploiting these different kinematic dependences. In practice, however, this task is probably not feasible given realistic beam time considerations. Thus, we turn to model estimates for guidance as to the magnitudes of the various LEC's. Theoretical values for  $h_\pi^1$  and  $h_V$  have been discussed elsewhere, and one finds no strong *a priori* reason to conclude that they differ significantly in magnitude[20]. For the magnetic LEC  $C$  we are not able to perform a first principles theoretical calculation of its size. We may, however, perform an estimate using a vector meson dominance picture involving  $t$ -channel  $\rho$ -exchange, wherein the parity violation arises from the PV  $\rho NN$  interaction. When the  $\rho$  meson is treated as a heavy degree of freedom and is integrated out, we find the contact effective Lagrangian Eq. (10). The relevant diagram is shown in FIG. 3. For the  $\rho\pi\gamma$  vertex we use

the Lagrangian:

$$\mathcal{L}_{\rho\pi\gamma}^{PC} = e \frac{g_{\rho\pi\gamma}}{4m_\rho} \epsilon^{\mu\nu\alpha\beta} F_{\mu\nu} G_{\alpha\beta}^- \pi^+ + \dots \quad (15)$$

where  $G_{\alpha\beta} = \partial_\alpha \rho_\beta - \partial_\beta \rho_\alpha$ . From the  $\rho$  radiative decay width [25] we have  $|g_{\rho\pi\gamma}| = 0.6$ , and for the PV  $\rho NN$  interaction we follow Ref. [1]

$$\mathcal{L}_{\rho NN}^{PV} = \sqrt{2} \left( h_\rho^0 - \frac{h_\rho^2}{2\sqrt{6}} \right) [\bar{p} \gamma_\mu \gamma_5 \rho^+ n + H.c. + \dots] \quad (16)$$

Invoking VMD we have

$$C \sim \frac{g_{\rho\pi\gamma}}{\sqrt{2}} \frac{\Lambda_\chi F_\pi m_\pi}{m_\rho^3} \left( h_\rho^0 - \frac{h_\rho^2}{2\sqrt{6}} \right) \quad (17)$$

Numerically, the resulting ratio of  $C$  and  $h_\pi^1$  contributions to the asymmetry is

$$\sim 0.017 \left| \frac{h_\rho^0 - \frac{h_\rho^2}{2\sqrt{6}}}{h_\pi^1} \right| = 0.03 \quad (18)$$

where we have used the "best values"  $h_\rho^0 = -30g_\pi$ ,  $h_\rho^2 = -25g_\pi$ ,  $h_\pi = 12g_\pi$  [1]. Thus, within the accuracy of our truncation, it appears that one may safely neglect the contribution generated by the interaction in Eq. (10).

One can obtain an experimental constraint on  $h_\pi^1$  from analysis of a nonradiative PV process. Up to now, however, there exists no such constraint on the magnitude of  $h_V$ . A determination of  $h_V$  would have both intrinsic interest as well as practical consequences for the interpretation of other experiments. As noted in Ref. [20], the presence of  $h_V$  in the nucleon anapole moment – coupled with the present lack of an experimental constraints on this constant – generates considerable theoretical uncertainty in the axial vector radiative corrections to PV  $ep$  scattering. Indeed, the numerical coefficient of  $h_V$  in  $R_A$  is twice as large as the coefficient of the PV  $\rho NN$  couplings. Given the constraints on the latter from PV  $\bar{p}p$  scattering, the PV  $\rho NN$  couplings give rise to the largest known hadronic effect. It is possible, however, that the  $h_V$  contribution is of similar strength. A determination of this LEC from PV pion photoproduction would undoubtedly aid in the interpretation of the SAMPLE result. More generally, the surprising importance of the subleading contribution to  $A_\gamma$  involving  $h_V$  suggests careful scrutiny of subleading chiral corrections to other PV radiative processes. The deeper reasons for the importance of subleading chiral corrections in this context as well as others involving hadronic PV [20, 19] is a subject for further study.

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## Figure Captions

Figure 1. The relevant Feynman diagrams for PV  $\pi^+$  photoproduction. The circle filled with a cross is the PV vertex.

Figure 2. The  $\theta$ -dependence of  $A_\gamma(\omega = 160 \text{ MeV})$  associated with various PV sources. The solid, long-dashed, and short-dashed curves give kinematic dependences of the coefficients of  $h_\pi^1$ ,  $h_V$ , and  $C$ , respectively.

Figure 3. The t-channel  $\rho$ -meson exchange diagram used to estimate the PV LEC  $C$ .

